

**e-Epidemic models on interaction between malicious codes and anti-virus software**

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**INTRODUCTION**

- ❖ A year or two year before computer viruses spread through email and EXE file
- ❖ Now preferred way of spreading malware is by drive-by-drive download or email spam connecting through link
- ❖ Transmission of malicious objects in computer network is epidemic in nature

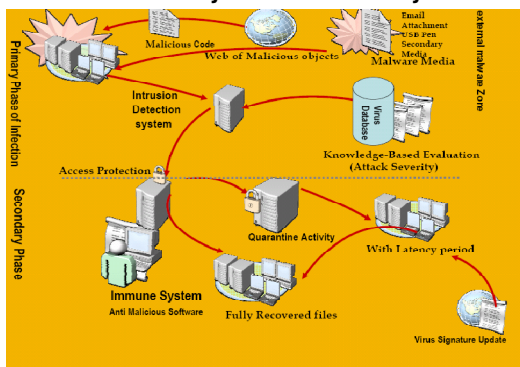
**INTRODUCTION**

- ❖ Attacking nature is different for different types of malicious code
- ❖ Different nature or classification of computer malware exist
- ❖ The study of computer may help to control infectious disease emergence
- ❖ Different kind of viruses exist like 'Logic Bomb', 'Parasitic'

**INTRODUCTION**

- ❖ Malicious code is treated through a model which comprise of IDS (Intrusion Detection System), ADS and Knowledge based system vulnerability information system
- ❖ The model is described in the next slide

**Virus attack cyber defense analysis**



**BASIC TERMINOLOGIES**

- ❖ **Computer virus** is a program that can "infect" other programs by modifying them to include a possibly evolved version of it
- ❖ **Antivirus (or "anti-virus") software** is a class of program that searches your hard drive and floppy disks for any known or potential viruses.
- ❖ **Quarantine:** To move an undesired file such as a virus-infected file or spyware to a folder that is not easily accessible by regular file management utilities.

### What are malicious objects?

- ❖ The term "gateway" refers in the art to a bridge between two networks. For each network, the gateway is a point that acts as an entrance to another network
- ❖ As a filtering facility, a gateway server has to be dealt with two contradicting objects: on the one hand, it has to hold a file that reaches the gateway in its path from a source to a destination until the inspection indicates it is harmless and thereby prevents its execution on the destination site, on the other hand holding a file at the gateway server until the inspection process terminates which results in a bottleneck to data traffic passing through the gateway. Inspection activity has a substantial influence on the traffic speed through a gateway

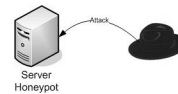
### What are malicious objects??

- ❖ Obviously hiding presence of a malicious program is more advanced than the non-hidden attack. The big threat it poses is the invisibility. The hidden process won't be seen in Task Manager. Beyond that the ordinary anti-spyware and anti-virus tool are not able to detect them either

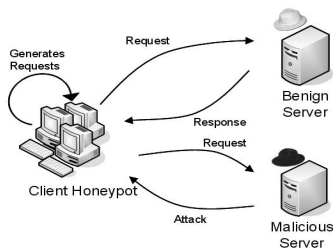
### What is malicious objects??

- ❖ At the heart of this vulnerability is the violation of trust that results from the "injected" script or HTML running within the security context established for the example.com site. It is, presumably, a site the browser victim is interested in enough to visit and interact with in a trusted fashion. In addition, the security policy of the legitimate server site example.com may also be compromised.

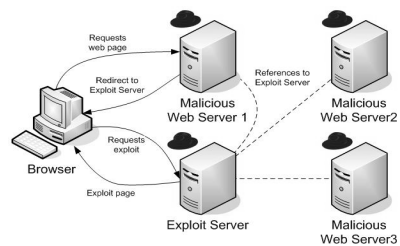
### Malicious objects-Facts



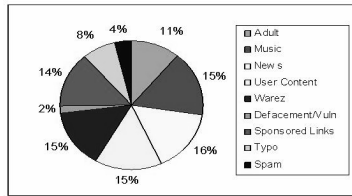
### Malicious objects-Facts



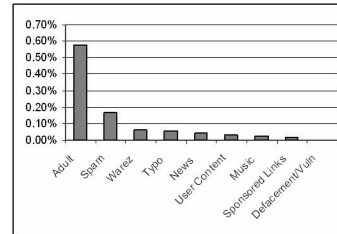
### Malicious objects-Facts



### Malicious objects-Facts



### Malicious objects-Facts



#### DEVELOPMENT OF THE MODEL

- ❖ Set of Instructions written by the User to harm the system is said to be the 'Virus' which attack the computer
- ❖ Some of the virus self-replicating in nature
- ❖ Some of them enter in the latent class and reactivate after certain duration
- ❖ Antivirus software immune the system if it is attacked by the virus

#### DEVELOPMENT OF THE MODEL

- ❖ During immunization some of the infected files get fully recovered, whereas, some of them are quarantined (or suppressed), may be due to the lower version of the antivirus software installed.
- ❖ Then for this situation a higher version or new antivirus software is run to get a full recovery
- ❖ We try to develop Mathematical models for these situations

#### DEVELOPMENT OF THE MODEL

- ❖ Virus is replicated by the infected files.
- ❖ Viruses die at a specific rate  $b$ . Death of a virus equivalently mean to say the complete recovery of infected files from virus when antivirus software is run in the computer node for a specific session.
- ❖ The uninfected files are constantly being produced or developed by the users at a rate  $c$ .
- ❖ Uninfected files die at a constant rate  $d$  (natural death). Death of a file equivalently mean to say that the file become irrelevant (garbage) after a certain interval of time.

#### DEVELOPMENT OF THE MODEL

- ❖ Infected files die at a specific rate, where  $d$  is natural death rate and  $e$  the death rate of the file (files get damaged and unable to be recovered after the run of antivirus software) due to infection from the virus.
- ❖ Death of antivirus software equivalently mean to say the present version of the software is incapable of identifying the attack of new viruses.

### Model 1: Primary phase of an Infection

- ❖ Viruses get entry to the computer node via various means (emails, infected disks etc.) and hijack various files (command files, executable files, kernel.dll, etc.) in the node for its own replication.
- ❖ It then leaves a specific file and the process is repeated.
- ❖ Viruses may be of different nature and as per their propagation mode; they target different file types of the attacked computer for this purpose.

### Model 1: Primary phase of an Infection

$$\frac{dV}{d\tau} = aY - bV$$

$$\frac{dX}{d\tau} = c - dX - \beta XV$$

$$\frac{dY}{d\tau} = \beta XV - fY$$

### Model 1: Primary phase of an Infection

- ❖ Let X be the number of uninfected files (prey) and V be the number of computer virus (predators), then
- ❖ {Rate of change of X} = {net rate of growth of X without predation} - {rate of loss due of X to predation, and
- ❖ {Rate of change of V} = {net rate of growth of V due to predation} - {net rate of loss of V without prey}

### Model 1: Primary phase of an Infection

- ❖ Let,  $R_0$  be the basic reproductive ratio for the computer virus; defined to be the expected number of viruses that one virus gives rise to an uninfected file population. A virus gives rise to infected files at a rate  $\beta X$  for a time  $1/b$ , and each infected files gives rise to virus (self replication) at a rate  $a$  for a time  $1/f$ . since  $X=c/d$  for a uninfected population,

$$R_0 = \frac{\beta ca}{dbf}$$

The criterion for the spread of the computer virus is

$$R_0 > 1$$

### Model II: Secondary Phase of Infection (Effect of Immune system)

- ❖ We assume the response of the immune in the computer system due to antivirus software Z which are run at a constant rate  $g$  and  $h$  being the death rate of antivirus software
- ❖ The antivirus software cleans the infected files at a rate
- ❖ There is an analogy here of Z antivirus software as predators and Y infected files as prey
- ❖ We take linear functional response of Z to Y

### Model II: Secondary Phase of Infection (Effect of Immune system)

$$\frac{dV}{d\tau} = aY - bV$$

$$\frac{dX}{d\tau} = c - dX - \beta XV$$

$$\frac{dY}{d\tau} = \beta XV - fY - \gamma YZ$$

$$\frac{dZ}{d\tau} = g - hZ$$

### 3.3 Model III: Effect of new antivirus software on such viruses which are suppressed (quarantine)

We assume a case where the viruses are not completely cleaned (quarantine) from the infected files on run of installed antivirus software on the computer node. For the complete recovery of infected files from viruses, updated version of antivirus has to be run. Further we assume that such updated antivirus software is available and is 100% efficient. This antivirus software switches  $\beta$  to zero and thus the equations for the subsequent dynamics of the infected files and free virus from equation (1) is expressed as

$$\begin{aligned}\frac{dV}{d\tau} &= aY - bV \\ \frac{dX}{d\tau} &= c - dX \\ \frac{dY}{d\tau} &= -fY\end{aligned}$$

We further assume that the half-life of the virus is much less than that of the virus producing files. Then,

$$\begin{aligned}Y &= Y_0 e^{-ft} \\ V &= \frac{V_0 (be^{-ft} - fe^{-bt})}{(b-f)}\end{aligned}$$

From equation (14) we are able to say that the number of infected files falls exponentially. The behavior of  $V$  follows from the assumption on half-lives, so that

$$f \ll b$$

that is, the amount of free virus falls exponentially after a shoulder phase.

### Model IV: Reactivation of computer virus after they are in latent class

When computer virus attacks the computer node, some of them enter a latent class on their infection. While in this class they do not produce new viruses, but may later be reactivated to do so. Only the files in the productive infected class  $Y_1$  produce viruses, and files at latent infected class  $Y_2$  leave for  $Y_1$  at a per capita rate  $d$ . Thus our system becomes:

$$\begin{aligned}\frac{dV}{d\tau} &= aY_1 - bV \\ \frac{dX}{d\tau} &= c - dX - \beta XV \\ \frac{dY_1}{d\tau} &= q_1 \beta XV - f_1 Y_1 + \delta Y_2 \\ \frac{dY_2}{d\tau} &= q_2 \beta XV - f_2 Y_2 - \delta Y_2\end{aligned}$$

Infected files at class  $Y_2$  produce viruses in class  $Y_1$  at a rate  $\delta$  for a time  $\frac{1}{\delta + f_2}$

Thus adding the contribution of both the classes, the reproductive ratio  $R_0$  is expressed as

$$R_0 = \frac{\beta c}{db} \left( q_1 + q_2 \frac{\delta}{\delta + f_2} \right) \frac{a}{f_1}$$

**3.5 Model V: Recent Attack by malicious object Backdoor.Haxdoor.S and Trojan.Schoeberl.E and its Mathematical approach**

On January 9, 2007 Backdoor.Haxdoor.S and Trojan.Schoeberl.E malicious object of type Trojan Horse having infection length of 56,058 bytes affected Windows 2000, Windows 95, Windows 98, Windows Me, Windows NT, Windows Server 2003, Windows XP. Backdoor.Haxdoor.S is a Trojan horse program that opens a back door on the compromised computer and allows a remote attacker to have unauthorized access. It also logs keystrokes, steals passwords, and drops rootkits that run in safe mode. It has been reported that the Trojan has been spammed through email as an email attachment. The tool **FixSchoeb-Haxdoor.exe** is designed to remove the infections of Backdoor.Haxdoor.S and



FixSchoeb-Haxdoor.exe tool meant to remove the deadly Backdoor.Haxdoor.S and Trojan.Schoeberl.E prevent infected files from producing infectious virus. We assume that W are the un-infectious virus which start to be produced from the infected files Y after the tool FixSchoeb-Haxdoor.exe is run. Infectious virus are still present, and die as before, but are no longer produced. Under this assumption the system can be modeled as

**Discussion and Conclusion**

The threshold parameter obtained in (2) for primary phase of discusses the criterion for the spread of the computer virus, that

- The susceptible population X (uninfected files) is reduced by the virus until each virus is expected to give rise to exactly one new virus,
- The basic reproductive ratio in the presence of the immune system defined by (11) and in order for the immune response to control infection we need the immune response parameter  $K$  to satisfy  $K > \alpha(R_0 - 1)$

For the viruses which are quarantined by the installed antivirus software we assume that updated antivirus software is available and efficient. When this updated antivirus software is run, from equation we are able to say that the number of infected files falls exponentially. The behavior of V follows from the assumption on half-lives, so that

We assume that the uninfected file population X remains roughly constant for a given time-scale, that is,

$$X = X^* = \frac{bf}{a\beta} \quad \text{and that} \quad f \ll b$$

System (17) becomes a linear system which is integrated to have

$$V = V_0 e^{-br}$$

$$Y = Y_0 \frac{f e^{-br} - b e^{-fr}}{f - b} \quad , \text{when } f \ll b$$

$$W = W_0 \frac{b}{b-f} \left( \frac{b}{b-f} (e^{-fr} - e^{-br}) - f e^{-br} \right)$$

From (18) it is clear that the total amount  $V + W$

of free virus falls exponentially after a shoulder phase.

**Nomenclature**

- V : number of viruses in the computer
- X : number of uninfected target files
- Y : number of infected files
- A : Replicating factor
- B : Death rate of a virus
- C : Birth of uninfected files by users
- D : Natural Death of an uninfected file
- E : Death rate of infected files
- f = e + d
- $\beta$  : Infectious contact rate, i.e., the rate of infection per susceptible and per infective
- R0 : Threshold parameter
- Z : Response of antivirus software, which immunizes the system
- C : Rate at which antivirus software is run, which is

## DISCUSSION AND CONCLUSION

- ❖ The threshold parameter obtained for primary phase of infection discusses the criterion for the spread of the computer virus, that is,  $R_0 > 1$
- ❖ The susceptible population  $X$  (uninfected files) is reduced by the attack until each virus is expected to give rise to exactly one new virus,
- ❖ The basic reproductive ratio in the presence of the immune system is defined Model II and in order for the immune response to clear the infection we need the immune response parameter to be more than secondary phase of infection

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# THANK YOU